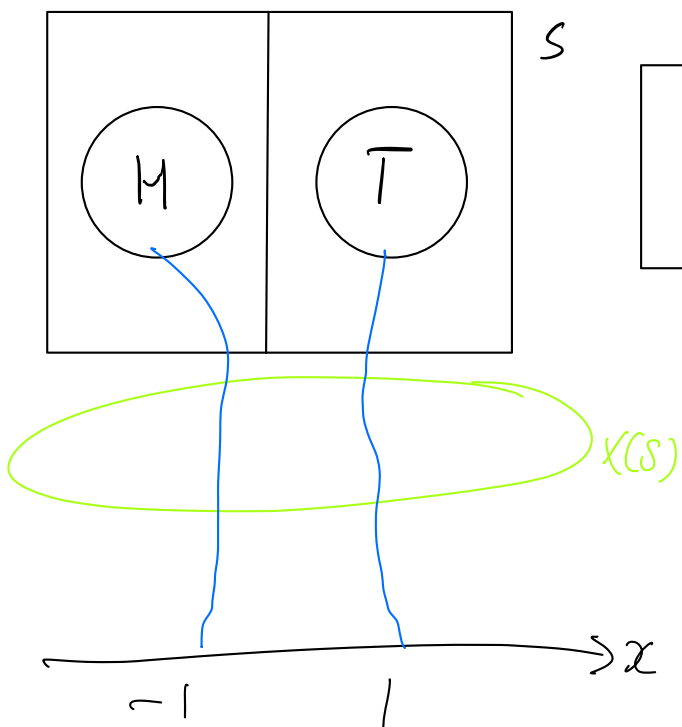


$$P(s_i) = \sim [0, 1]$$

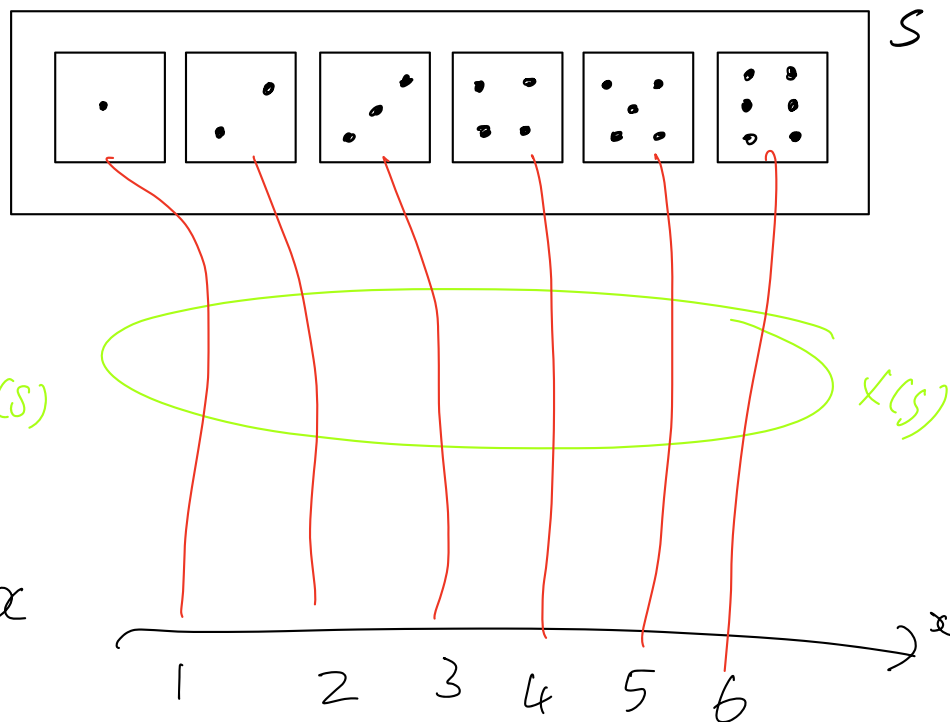
Random Variables

1. Flip a Coin



$$S_x = \{-1, 1\}$$

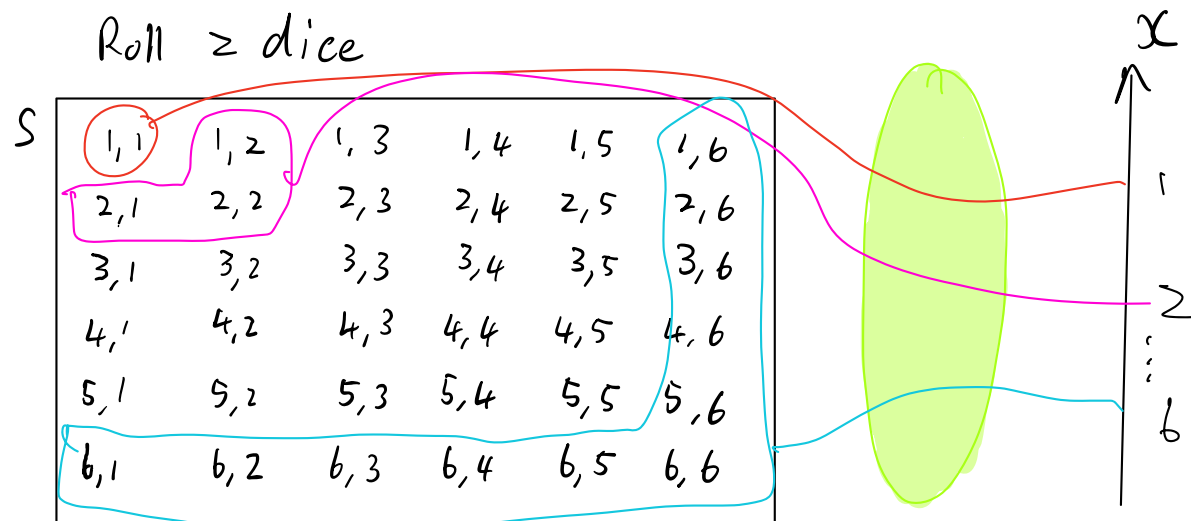
Roll a die



$$S_x = \{1, 2, 3, 4, 5, 6\}$$

2. A Function of the observation

Roll 2 dice



$$X(S) = \max \text{ of } 2 \text{ dice}$$

$$3. S_Y = \{1, 2, 3\}$$

$$X = 10 - 2Y$$

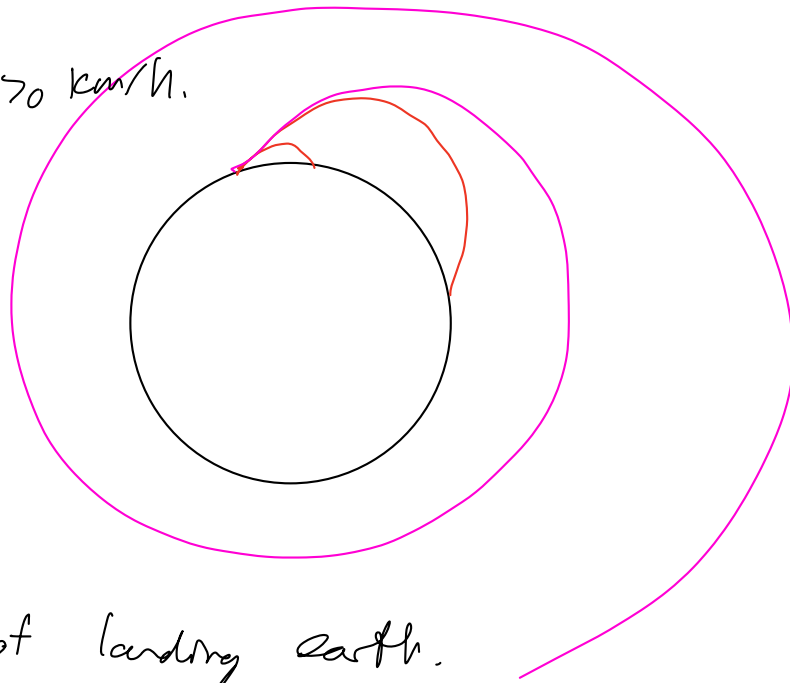
$$S_X = \{4, 6, 8\}$$

Improper experiment

Rocket fired with velocity V (in km/h).

What is time (T) in seconds that the rocket takes to land on the earth?

$$V > \sqrt[2]{v}^* = 40 \approx 70 \text{ km/h.}$$



• Probability of landing earth.

• T in seconds to land | landed on earth

1. Roll 6-sided die. $S_X = \{1, 2, 3, 4, 5, 6\}$

2. Test 6 circuits, either acceptable (a) or rejected (r)

$$S_0 = a a a a a a$$

$$2^6 = 64 \text{ outcomes.}$$

$$S_8 = a a r a a a$$

$$S_{10} = a a r a r a$$

Define N number of acceptable circuits.

$$S_N = \{0, 1, 2, 3, 4, 5, 6\}$$

3. Define R as revenue for batch of 6 ICs with

- $R50$ if acceptable (a)
- $-R70$ if rejected (r) — Customer support + replacement

if N is number acceptable
and $(6-N)$ is number rejected
then revenue (R) is as follows:

$$\begin{aligned} R = g(N) &= 50N - 70(6-N) \\ &= 120N - 420 \end{aligned}$$

$$r_8 = 120 \cdot 5 - 420 = R180$$

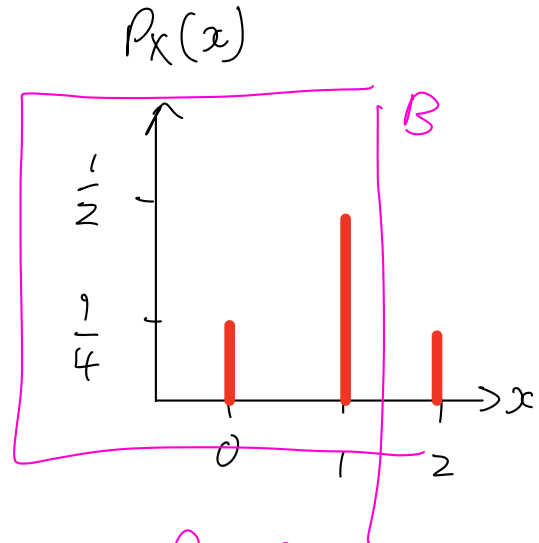
$$r_{10} = 120 \cdot 4 - 420 = R60$$

Example 3.5

Outcomes	bb	bg	gb	gg
$P(\cdot)$	$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{4}$
$X = \text{Points}$	0	1	1	2

$$S_X = \{0, 1, 2\}$$

$$P_X(x) = \begin{cases} \frac{1}{4} & x=0 \\ \frac{1}{2} & x=1 \\ \frac{1}{4} & x=2 \\ 0 & \text{otherwise.} \end{cases}$$



$$\begin{aligned} P(B) &= P_X(0) + P_X(1) \\ &= \frac{3}{4} \end{aligned}$$

Quiz 3.2

a) $\sum_{n \in S_N} P_N(n) = 1$

$$\frac{c}{1} + \frac{c}{2} + \frac{c}{3} = 1$$

$$6c + 3c + 2c = 6$$

$$11c = 6$$

$$c = \frac{6}{11}$$

b) $P(N=1) = \frac{6}{11}$

c) $P(N \geq 2) = P_X(2) + P_X(3) = 1 - P(N=1) = 1 - \frac{6}{11}$
 $= \frac{\frac{6}{11}}{2} + \frac{\frac{6}{11}}{3} = 0,45$

d) $P(N > 3) = 0$

$$S_N = \{1, 2, 3\}$$

